

# **Simple Techniques for Estimating the Shear Strength and the Coefficient of Permeability of Unsaturated Soils**

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**Unsaturated Soil Engineering: Applications in Pavements**

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# *Today's Presentation*

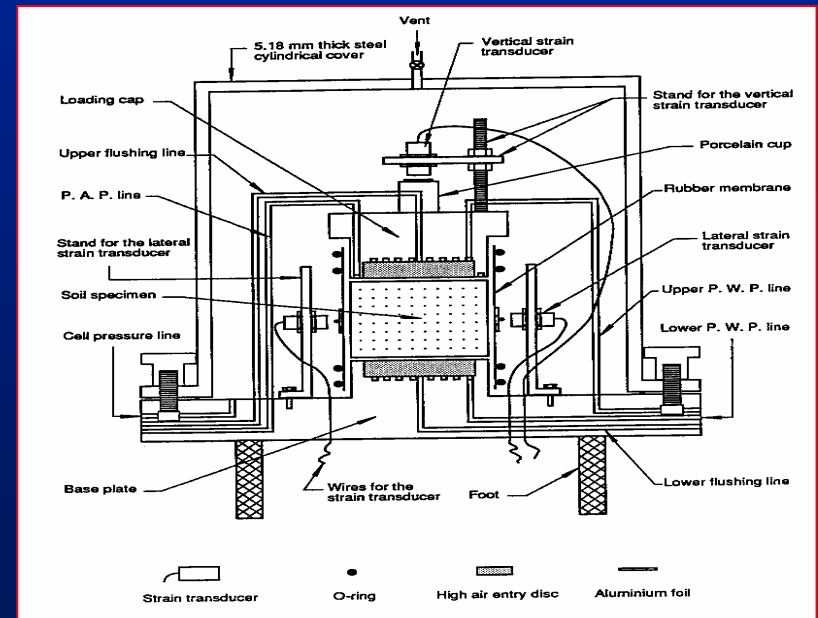
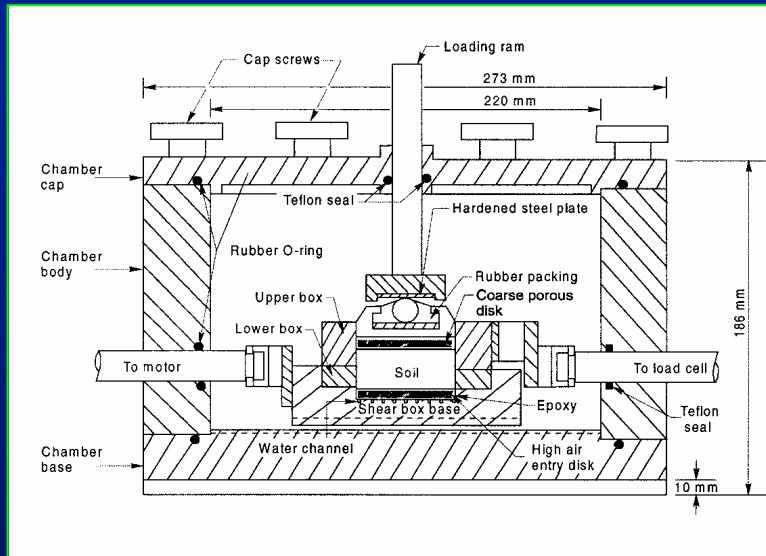
- **Establish:** Need for unsaturated soil mechanics in pavement designs
- **Theory:** Simple extensions of classical soil mechanics
- **Simple Techniques/Procedures for Interpreting the Engineering Behavior of Unsaturated Soils:** Using conventional soil mechanics lab facilities

# *Pavement Design Procedures*

- **Present /conventional procedures:** Experience and Empirical procedures
- **Rational procedure:** Take into account of the influence of wet-dry and freeze-thaw cycles (**Use principles of unsaturated soil mechanics**)
- **Rational Approach:** Use stress state variable approach (**Two stress state variables: Net normal stress,  $(\sigma - u_a)$  and matric suction,  $(u_a - u_w)$** )
- **Key engineering properties:** Shear strength and the Coefficient of permeability

# Unsaturated Soils Testing

## Shear Strength of Unsaturated Soils



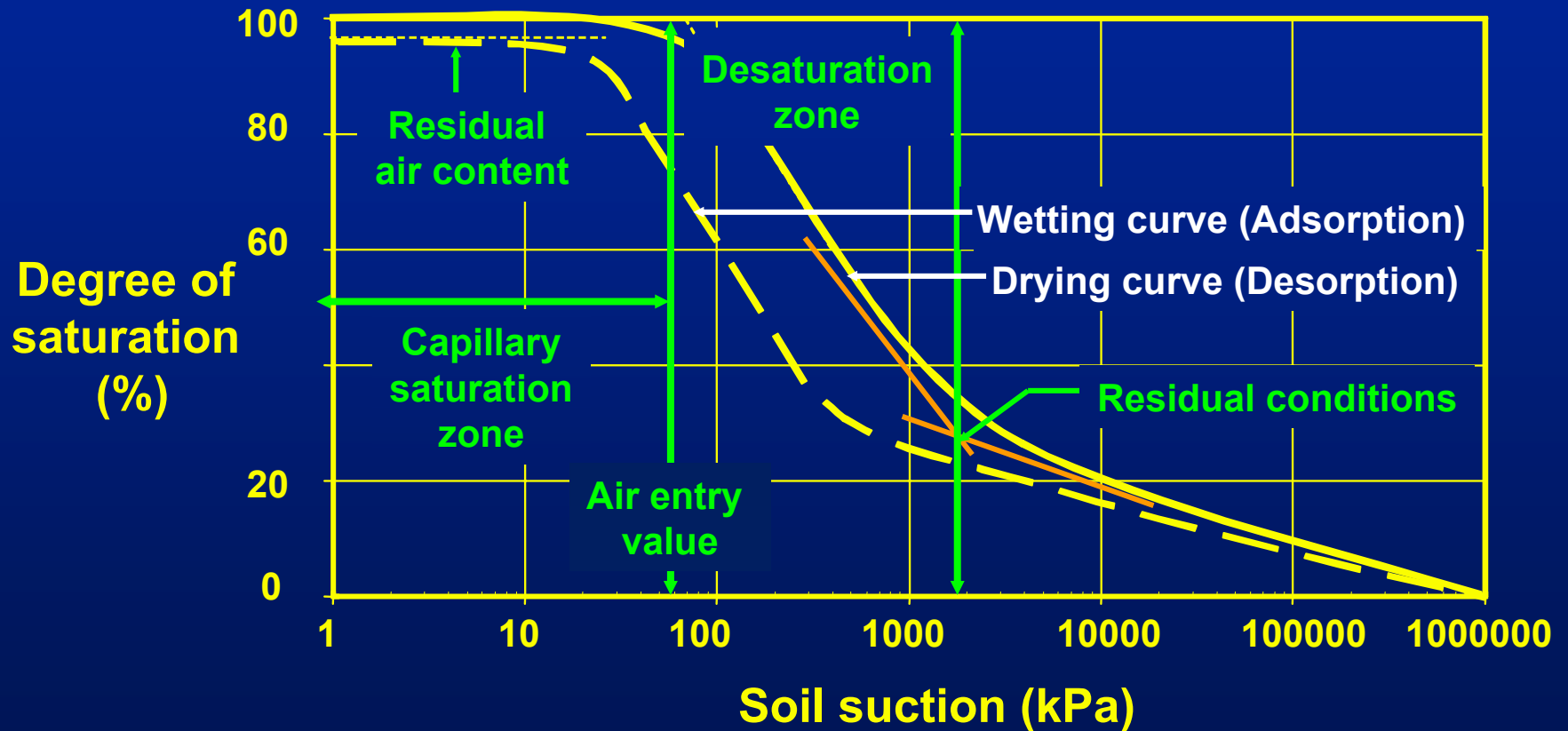
## Coefficient of Permeability of Unsaturated Soils

# *Unsaturated Soils Testing*

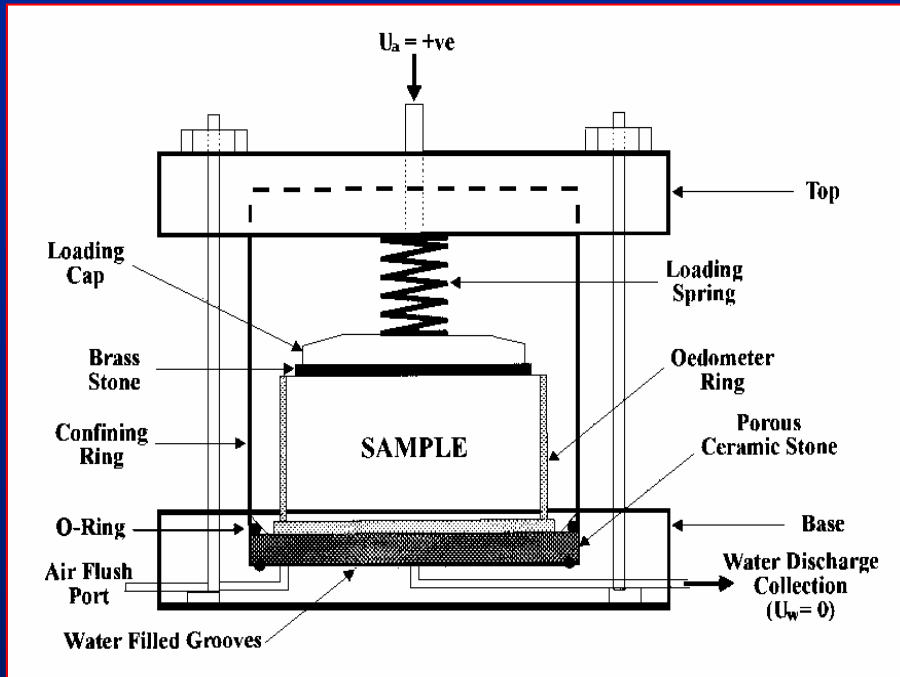
- Need extensive laboratory facilities
- Time consuming and expensive
- **Need simple techniques:** for practical applications such as the design of pavements
- **Focus:** Estimating the shear strength and the coefficient of permeability of unsaturated soils
- **Key information:** Soil-Water Characteristic Curve (SWCC)

# Soil-Water Characteristic Curve (SWCC)

*A useful tool in the interpretation of USM*



# Measurement of the SWCC



Tempe Cell/ Pressure plate  
(liquid phase flow)



Osmotic Desiccators  
(Vapor phase flow)

# ***Small - Scale Beckman Centrifuge J6 – HC***

**(Simple and fast technique  
for SWCC measurement)**





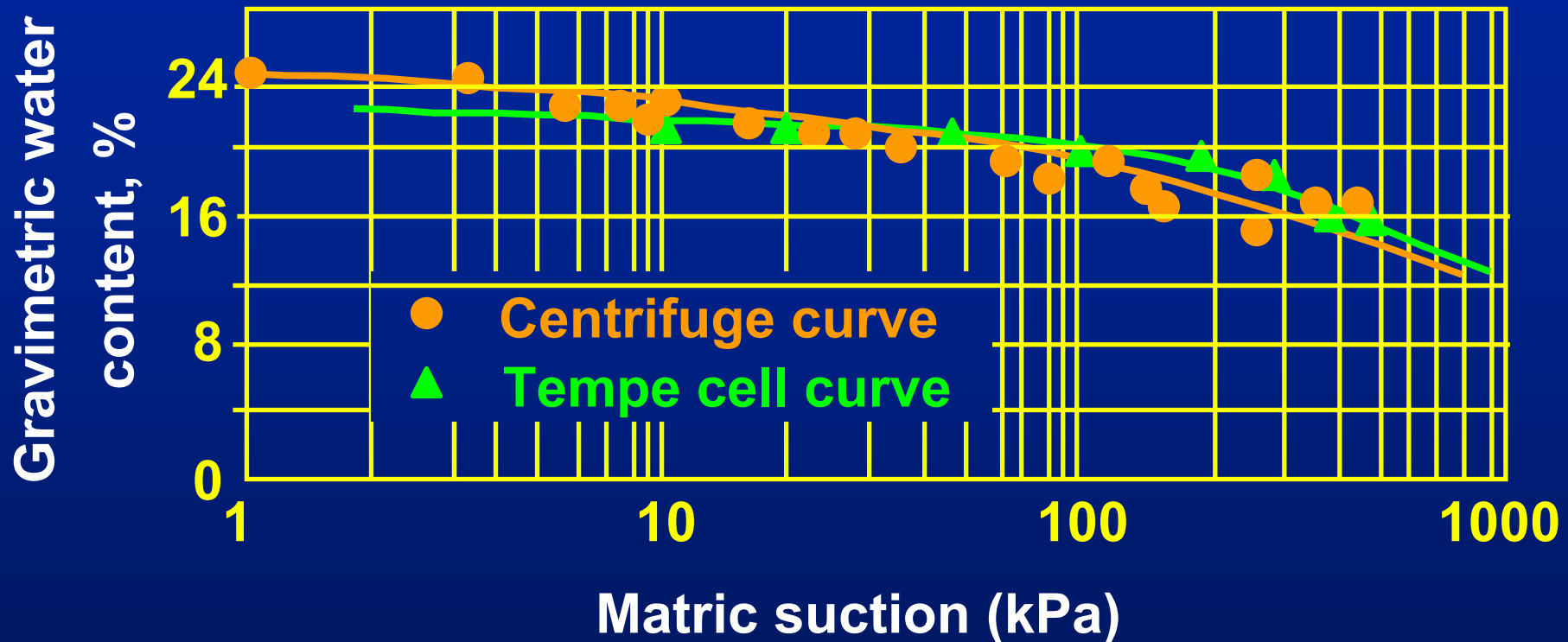
# ***Saturated Soil Specimens and Saturated Ceramic Cylinders in the Specimen Holders***



# ***Soil Specimen Holders Ready to Centrifuge***



# Indian Head Till Test Results



Centrifuge test,  $\rho_d = 1.77 \text{ Mg/m}^3$ ,  $w = 19.2\%$

Tempe cell test,  $\rho_d = 1.77 \text{ Mg/m}^3$ ,  $w = 19\%$

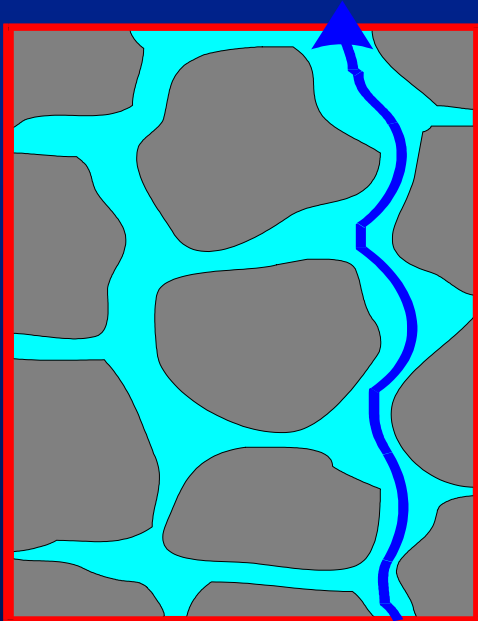
# ***Time Required to Obtain a SWCC***

<b>Test method used</b>	<b>Silt</b>	<b>Indian Head Till</b>	<b>Regina Clay</b>
<b>Centrifuge time (days)</b>	<b>0.5</b>	<b>1</b>	<b>2</b>
<b>Tempe cell time (days)</b>	<b>14</b>	<b>42</b>	<b>112</b>

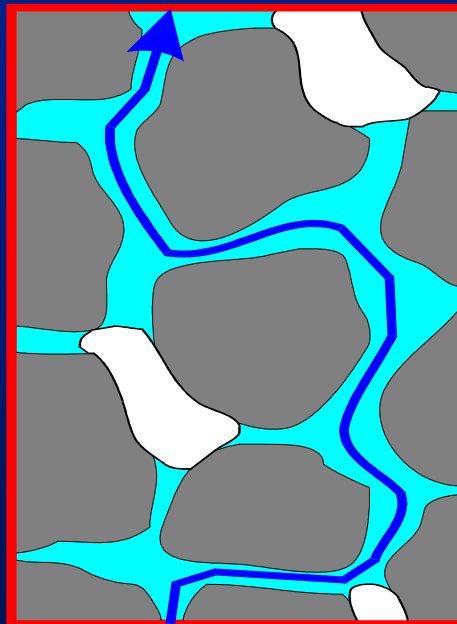
# *Pore Water Distribution*

Shear strength and Volume Change: Related to the interphase contact area controlling stress transfer

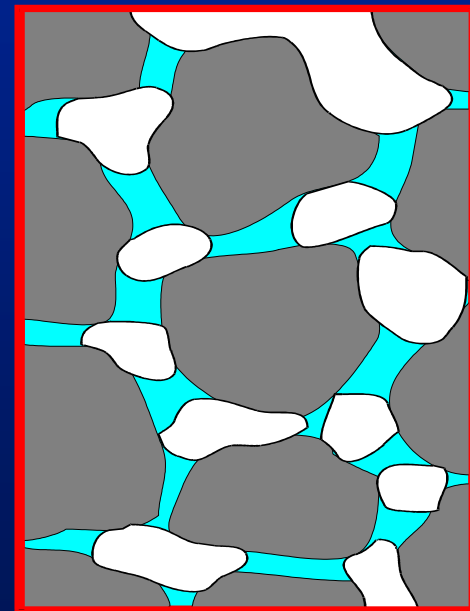
Coefficient of permeability : Related to the continuity and tortuosity of liquid phase



$$S = 100$$



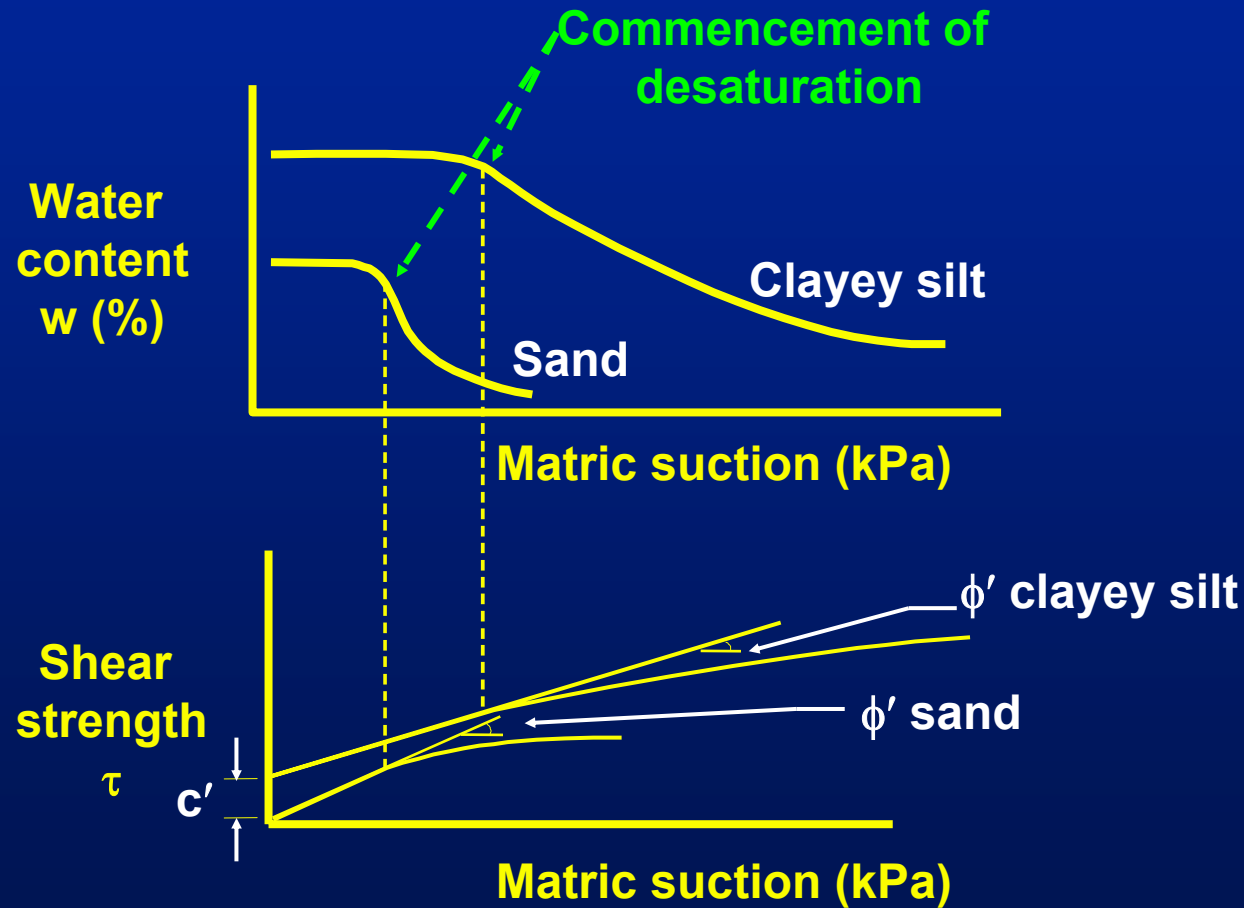
$$1 > S > S_r$$



$$S = S_r$$

# ***Shear Strength of Unsaturated Soils***

# Relationship Between SWCC and Shear Strength versus Matric Suction



# ***Unsaturated Soils Shear Strength Prediction (Vanapalli et al. 1996)***

$$\tau = c' + (\sigma_n - u_a) \tan \phi' + [\Theta(\psi)]^\kappa (u_a - u_w) \tan \phi'$$

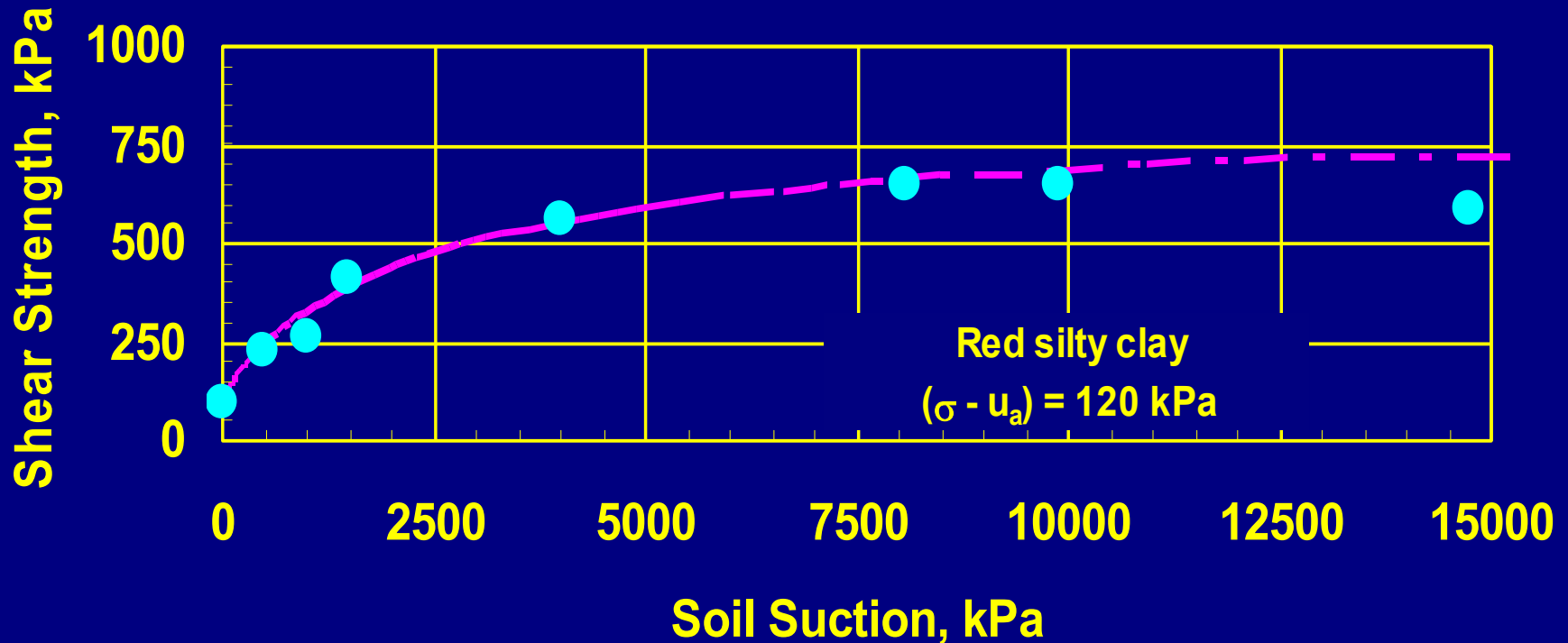
**where:  $\Theta(\psi) = \theta(\psi)/\theta_s$**

**$\theta(\psi)$  = volumetric water content at any suction**

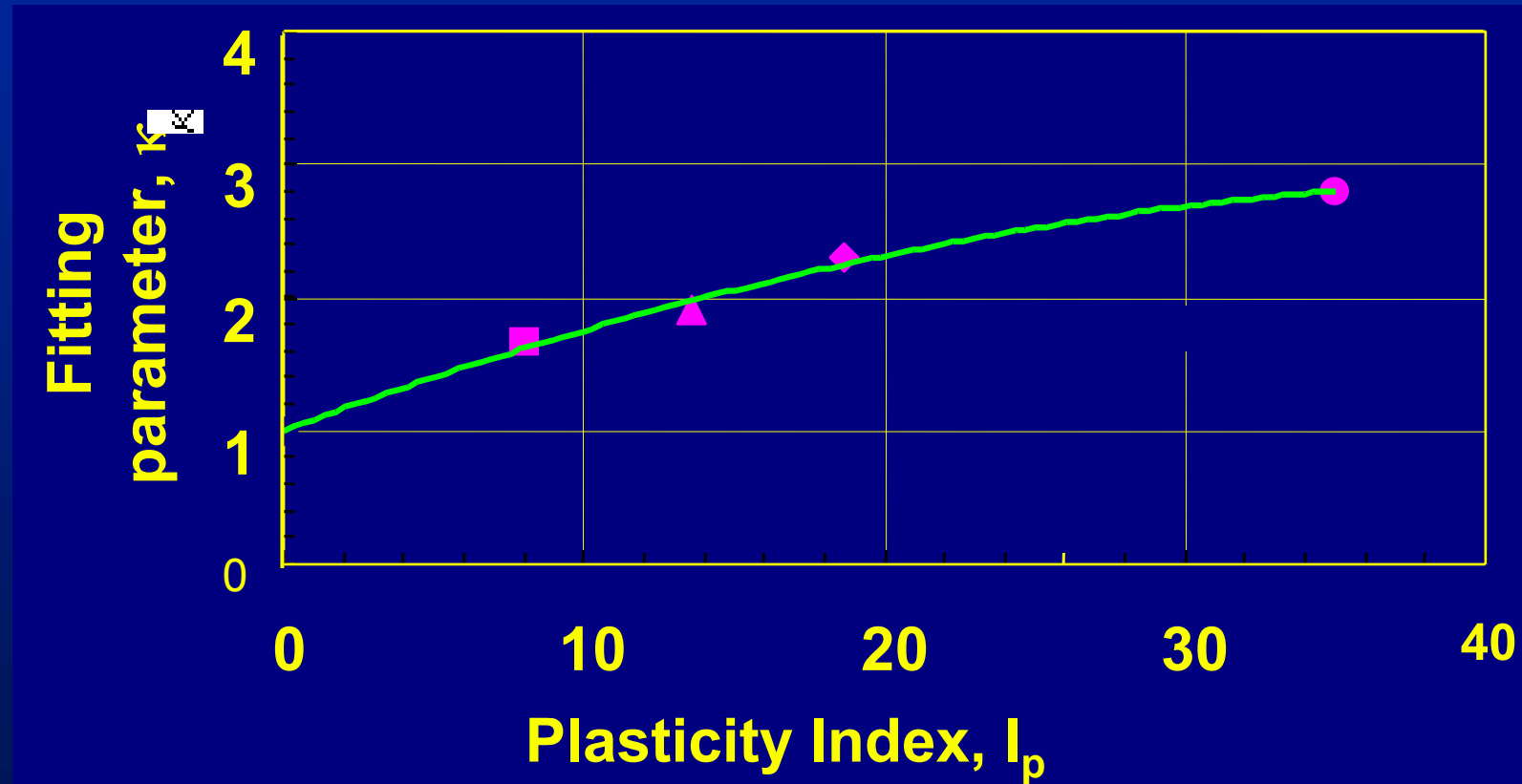
**$\kappa$  = fitting parameter to account for non-linearity between area and volume representation of the amount of water contributing to the shear strength**



# Comparison between Predicted and Measured Shear Strengths (Vanapalli and Fredlund, 2000)

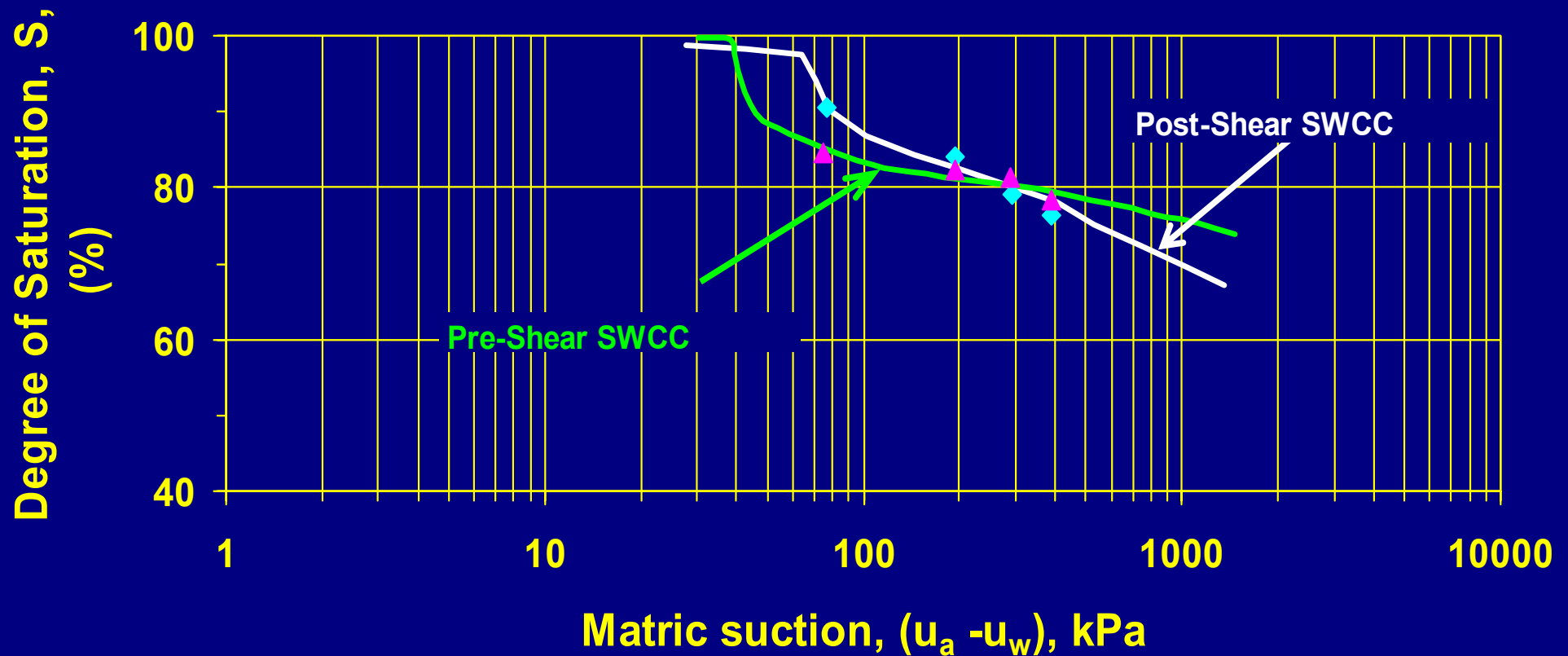


# Relationship between $\kappa$ vs $I_p$ (Vanapalli and Fredlund, 2000)

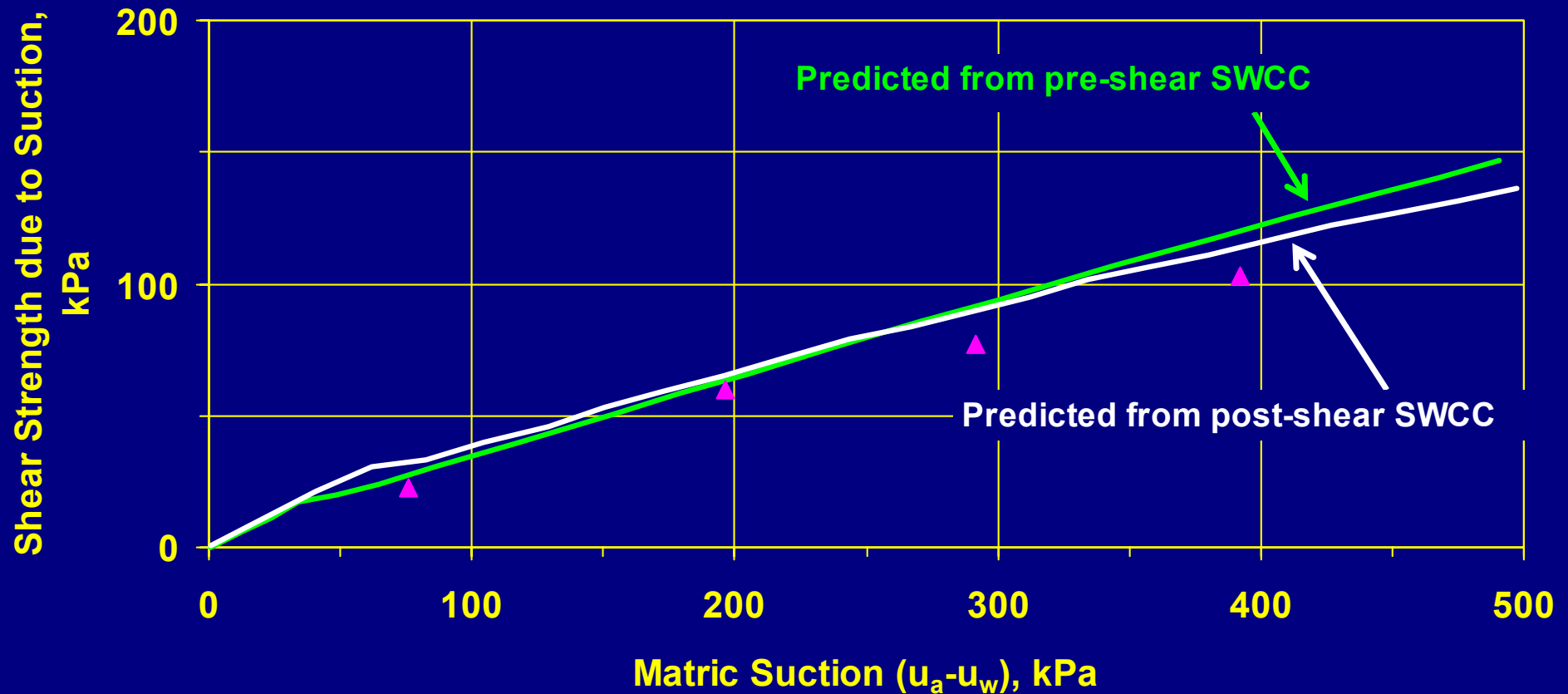


- Useful relationship to estimate the fitting parameter value,  $\kappa$

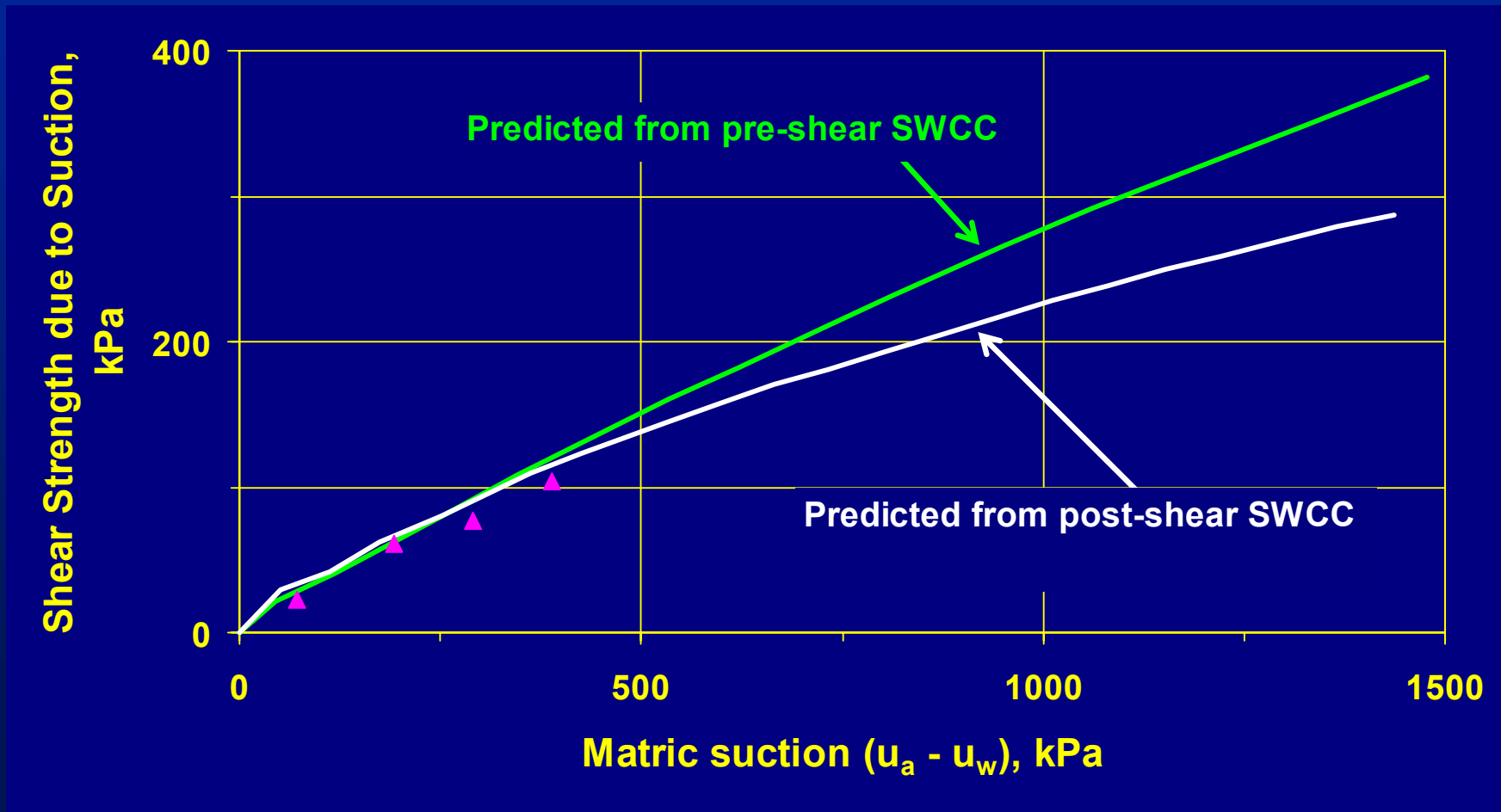
# Pre-shear and Post-shear SWCC data from the Triaxial Shear Test Results on Dhanauri clay specimens (derived from Satija 1978)



# Measured and Predicted Shear Strength of Dhanauri clay for Low Suction Range (Using Pre and Post-shear SWCC)



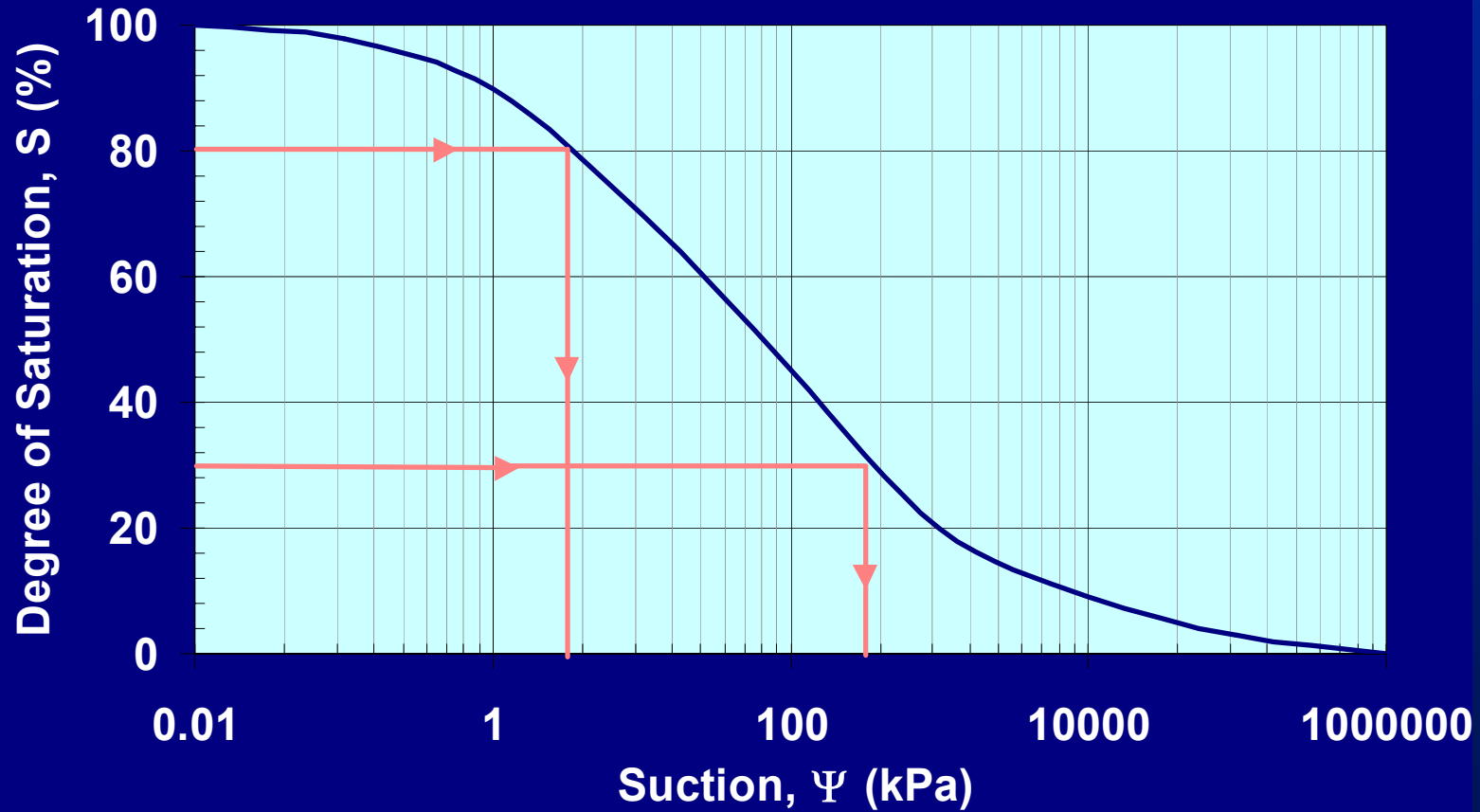
# Measured and Predicted Shear Strength of Dhanauri clay for High Suction Range (Using Pre and Post-shear SWCC)



# *Simple Test Procedures*

- **Conventional test procedures:** Unconfined compression test and Direct shear tests
- **Estimate of soil suction from simple tests?**  
Based on indirection estimation:
  - Determine the degree of saturation (from volume-mass properties)
  - Use SWCC information and estimate suction for corresponding degree of saturation

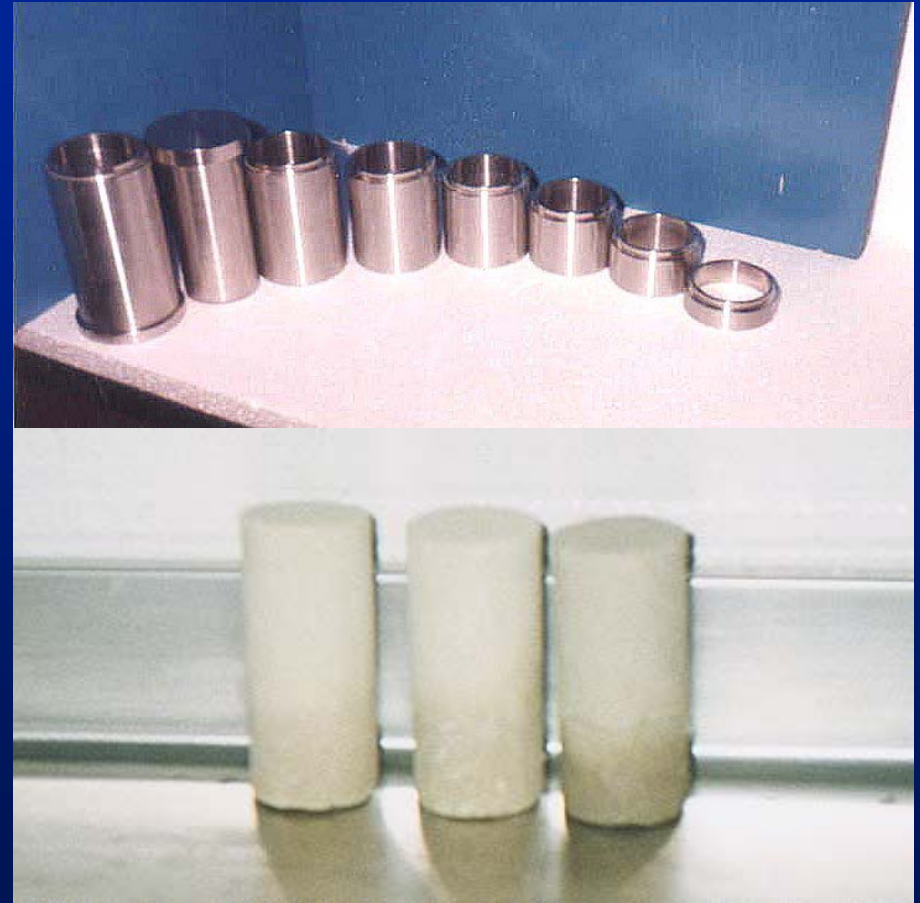
# *Estimation of Suction from the SWCC*



# **Shear Strength Interpretation from Unconfined Compression Test Results**

**(53<sup>rd</sup> Canadian Geotech Conf: Vanapalli et al. 2000)**

- Specimen preparation for a silt specimen ( $I_p = 8$ )
  - statically compacted saturated specimens prepared using constant volume molds
  - air dried for varying time intervals so that fully saturated to fully dry samples would be tested
  - suctions estimated from SWCC



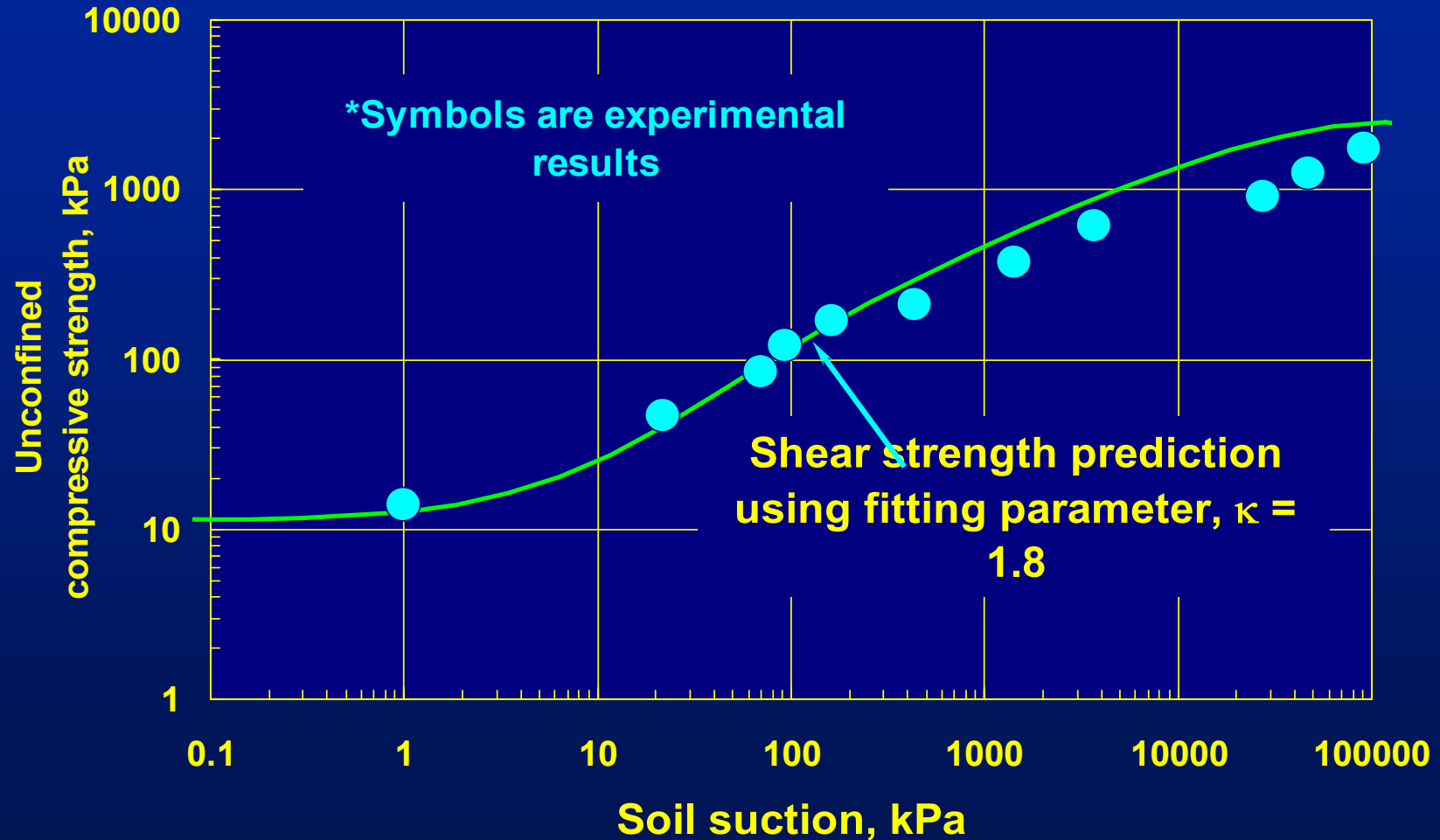


# ***Unconfined Compression Test***

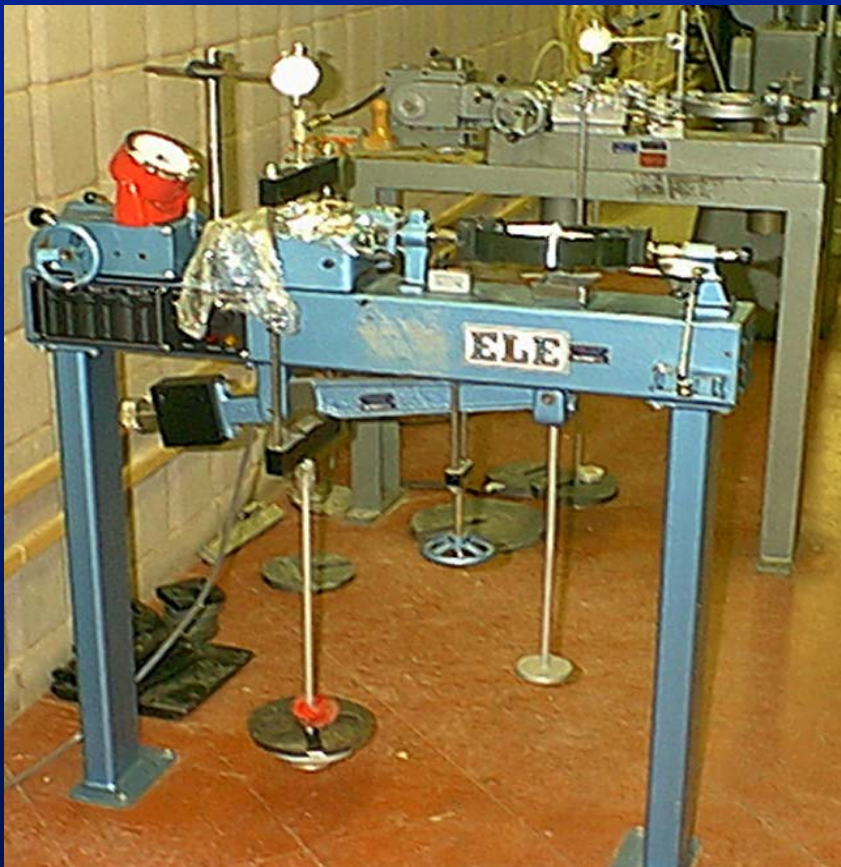


- **Testing**
  - Quickly loaded at a strain rate of approx. 1.2 mm/min
  - stress readings taken at every 0.2 mm interval travel
- **Assumptions**
  - Suction in the specimen does not change during loading
  - Interpretation based on initial suction values in the specimens

# Predicted and Measured Unconfined Compressive Strengths (Silt)

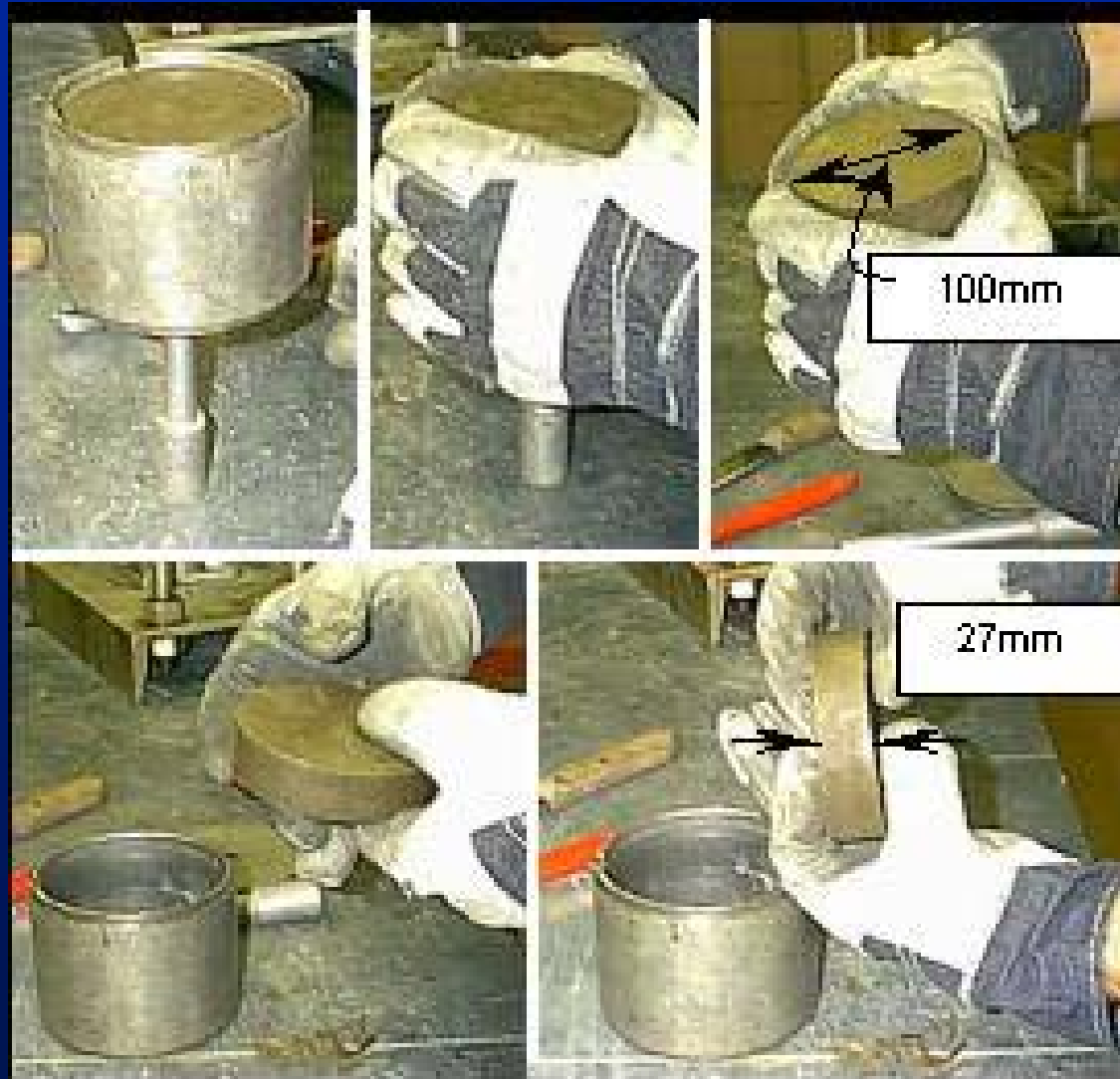


# ***Determination of Shear Strength of Compacted Till Using Conventional Direct Shear Apparatus (Vanapalli & Lane 2002)***



- **Shear strength of Indian Head till**
  - Three different compaction water contents
  - Provide comparisons between CDST and MDST
- **Assumption**
  - Suction in the specimen does not change during loading

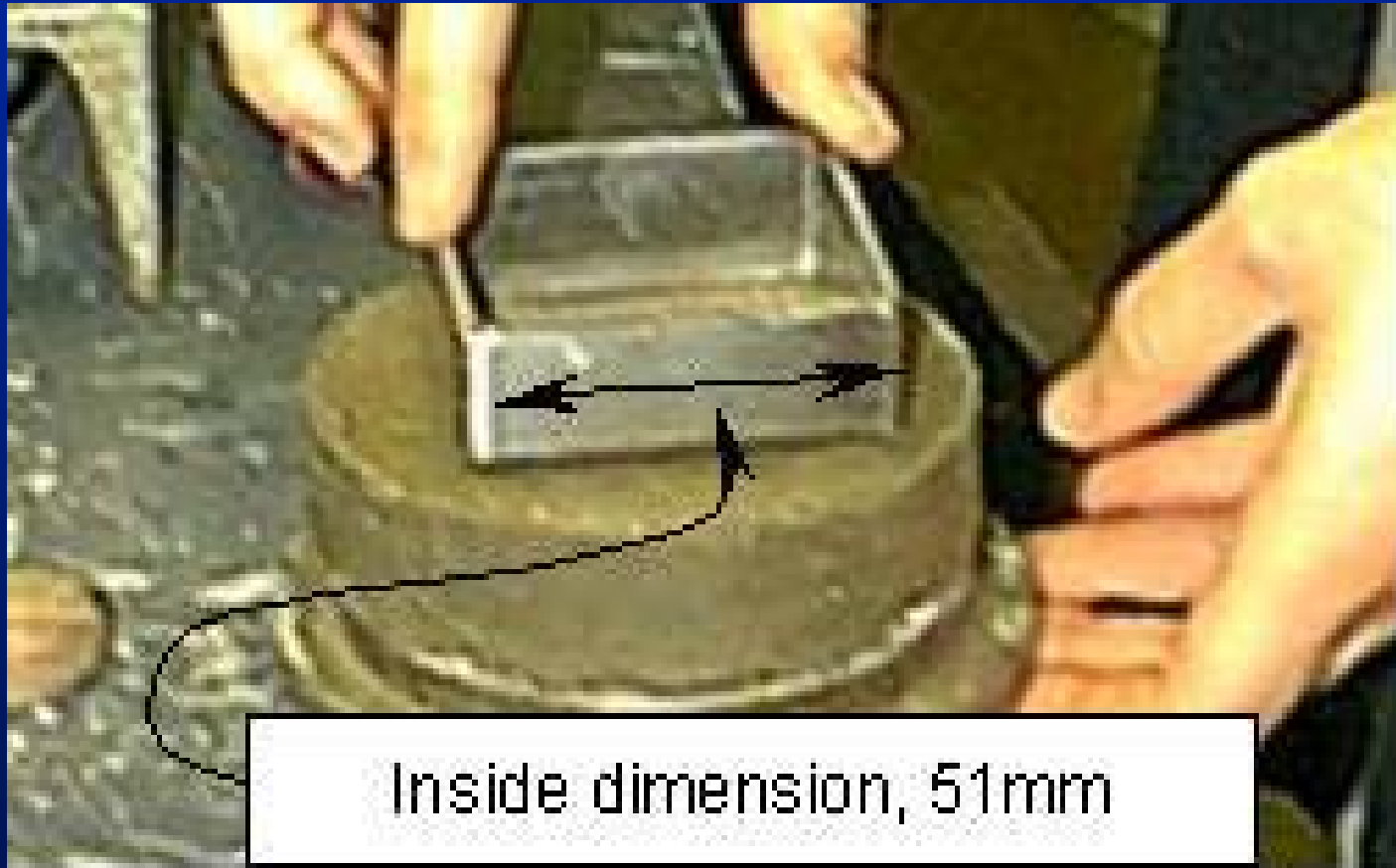
# Compacted Soil Specimen Extraction from Constant Volume Mould



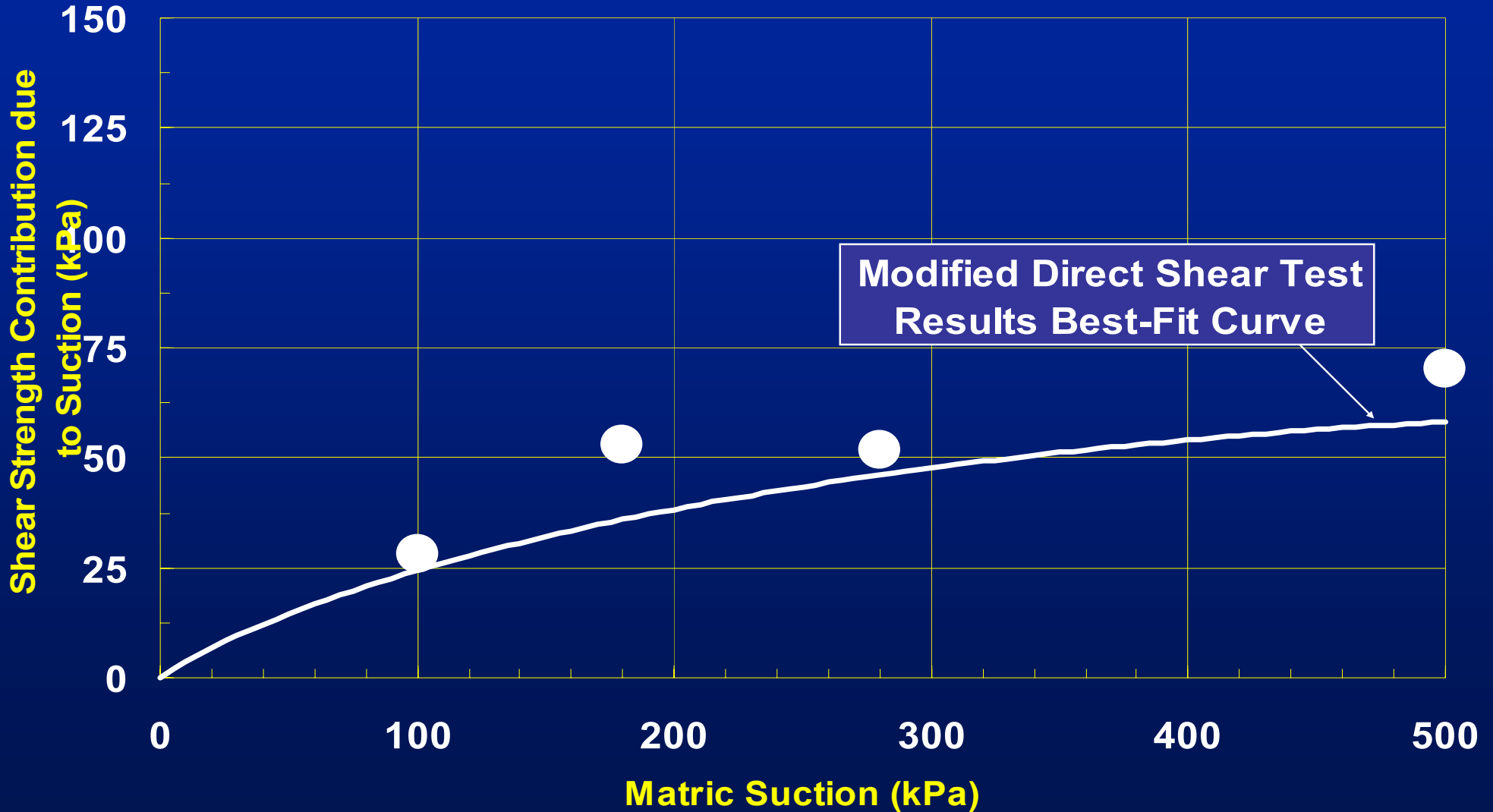
# ***Soil Specimen Saturation Procedure***



# *Soil Specimen & Cutter*



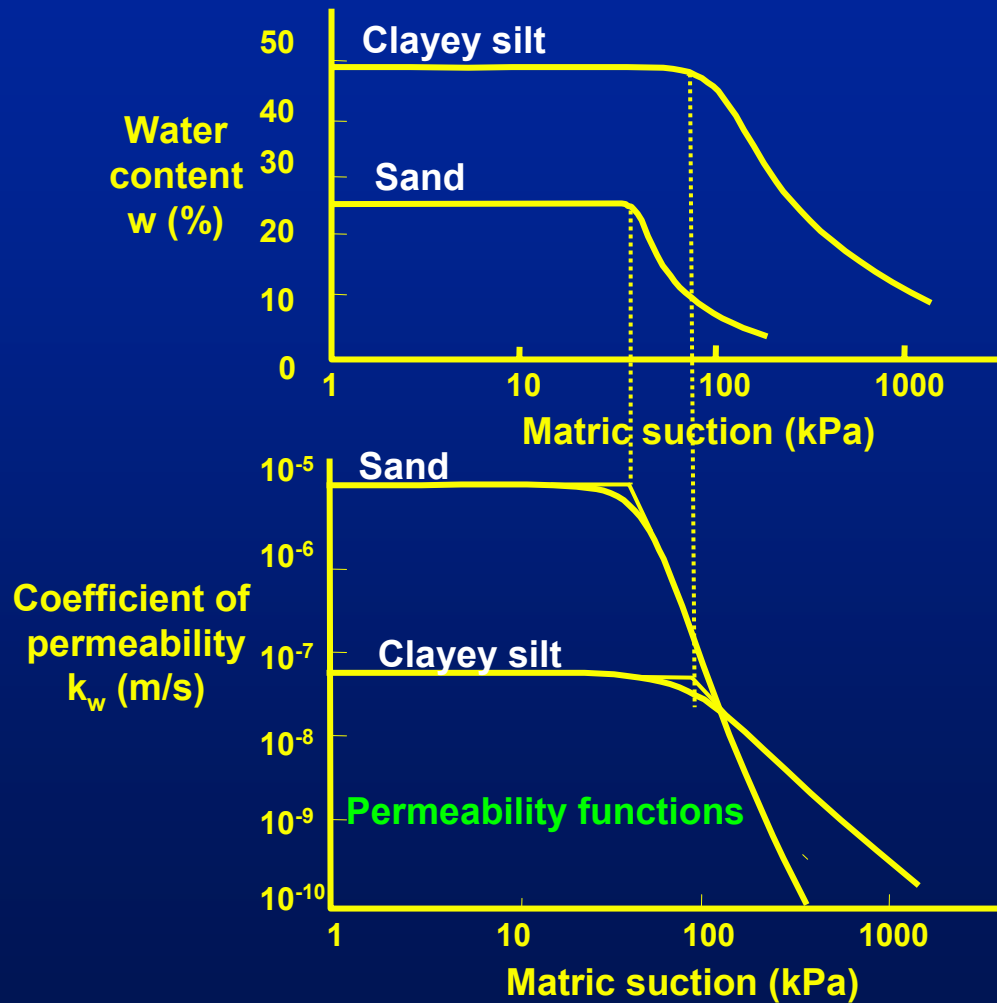
# Comparison between Shear Strength Test Results Using MDST and CDST (Vanapalli & Lane 2002)



***Coefficient of Permeability of  
Unsaturated Soils***



# Relationship Between the SWCC and Coefficient of Permeability



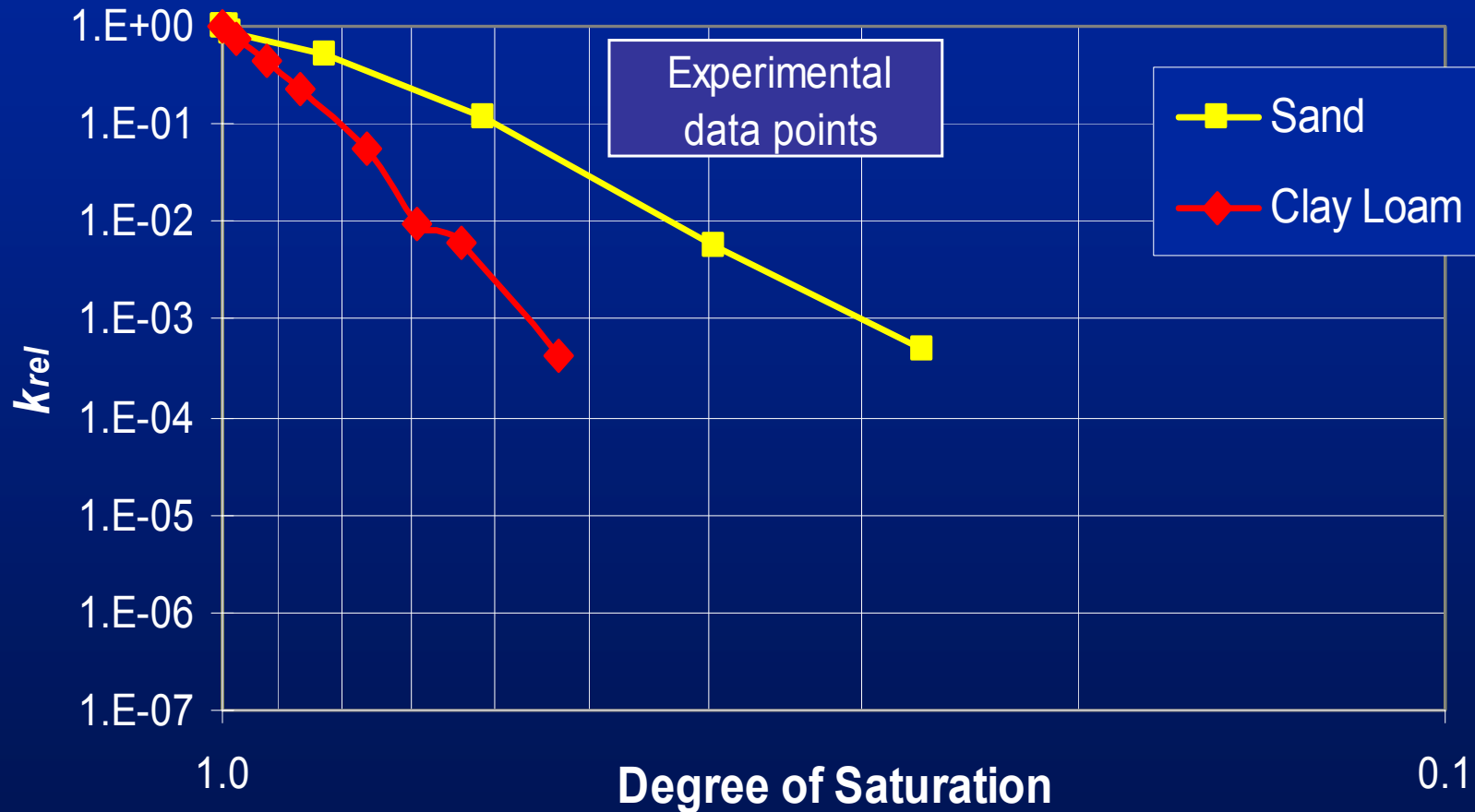
# *Predicting the Unsaturated Coefficient of Permeability of Soils*

- Several procedures available in the literature
- **Key information:** SWCC and  $k_{\text{sat}}$
- Several parameters influence the SWCC and the  $k_{\text{unsat}}$  :
  - applied stress
  - compaction energy
  - soil structure (function of initial compaction water content) (**important particularly in fine-grained soils**)

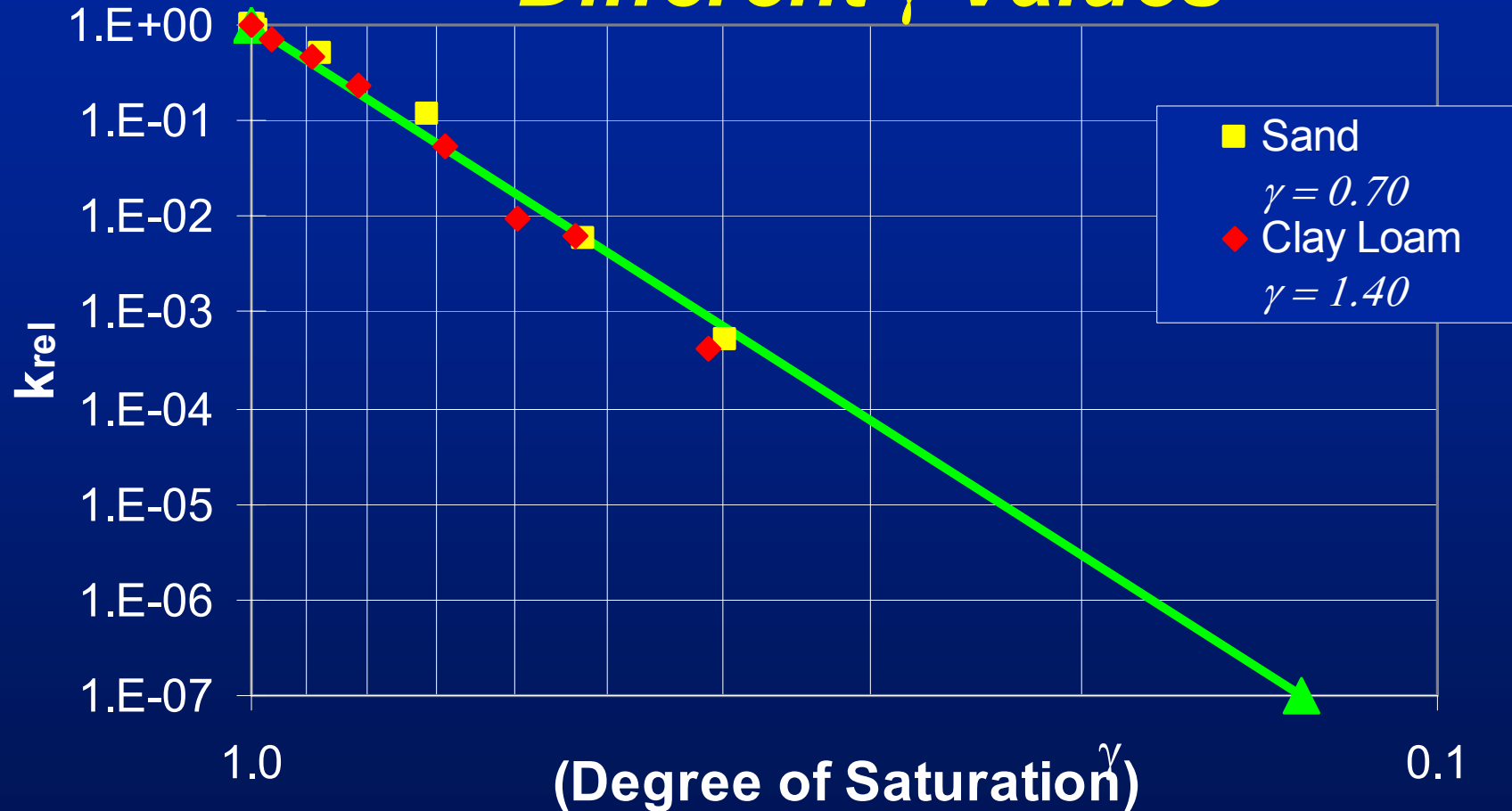
# ***Normalization Technique for Estimating the Coefficient of Permeability of Unsaturated Soils***

- Time consuming and expensive to measure SWCC taking into account the influence of parameters such as the stress state and soil structure
- Useful to the practicing engineers if a simple technique can be proposed.
- Relative or the normalized coefficient of permeability,  $k_{rel} = k_{unsat}/k_{sat}$

# Comparison of $k_{rel}$ and $S$ for a Typical Sand and Clay Loam

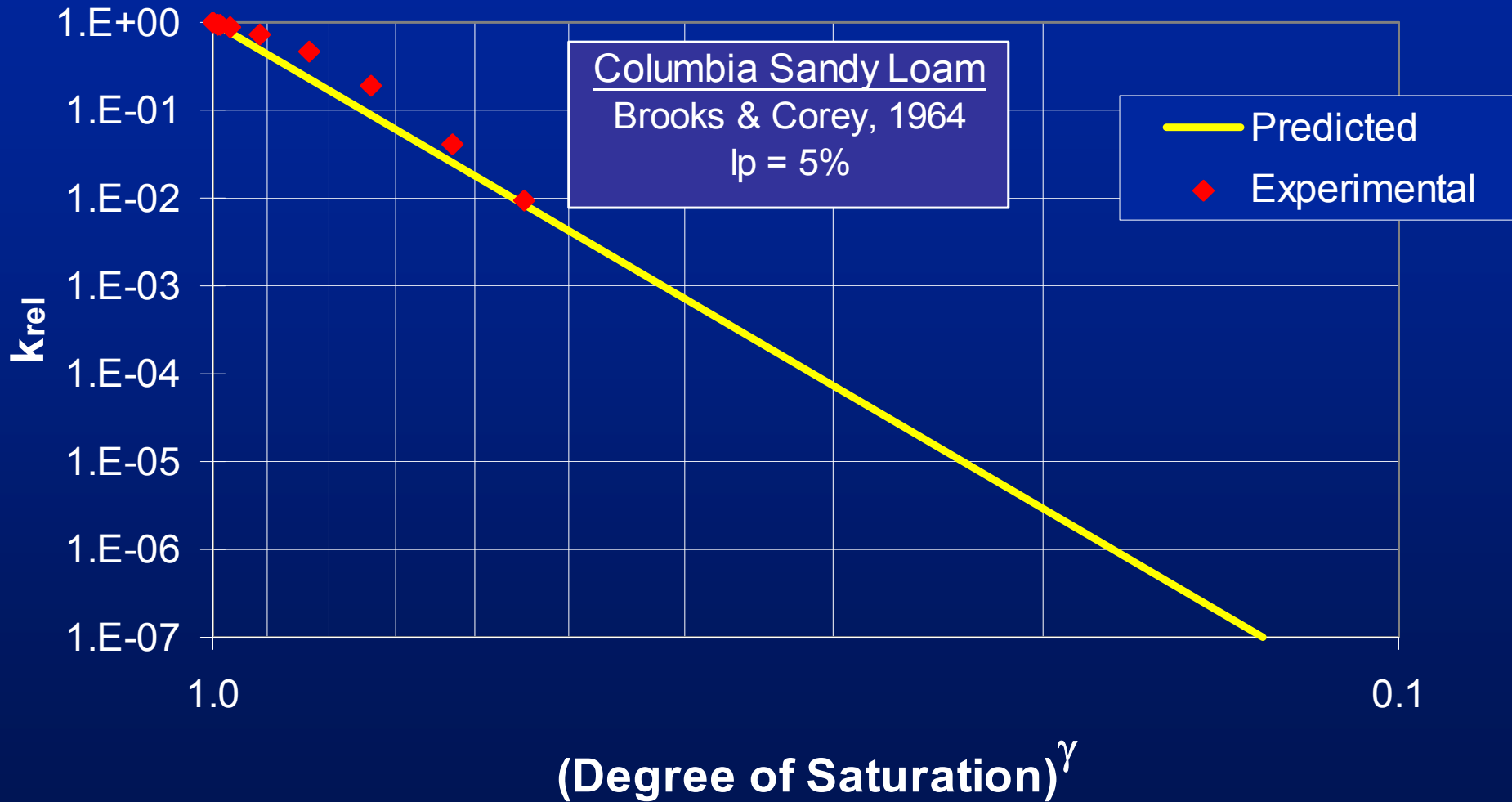


# $k_{rel}$ versus $S$ Using Different $\gamma$ Values

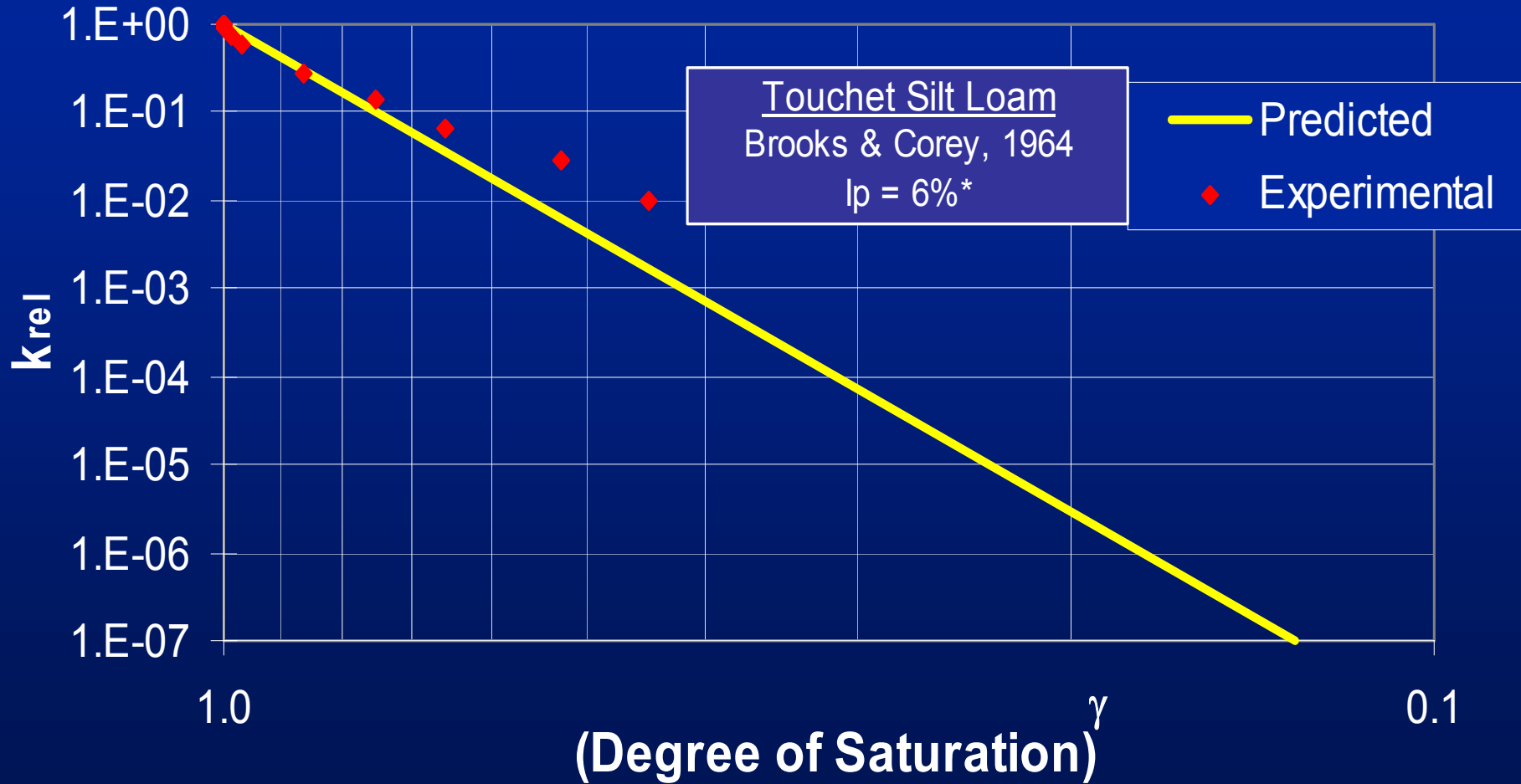


- Unique trend line for both the soils: Sand and Clay Loam through the use of different fitting parameter,  $\gamma$  values

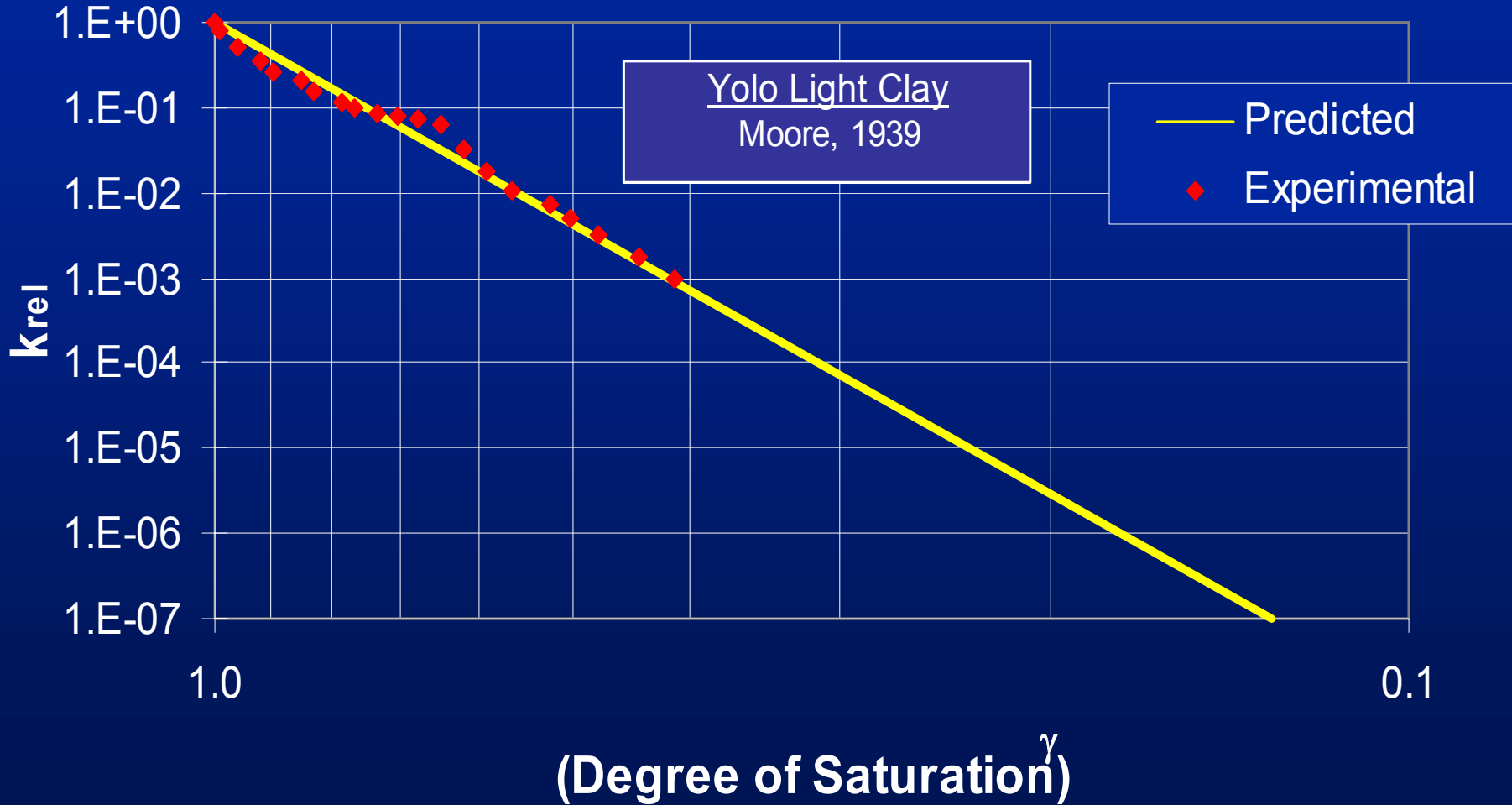
# $k_{rel}$ versus $S^\gamma$ for Columbia Sandy Loam



# $k_{rel}$ versus $S_r^\gamma$ for Touchet Silt Loam

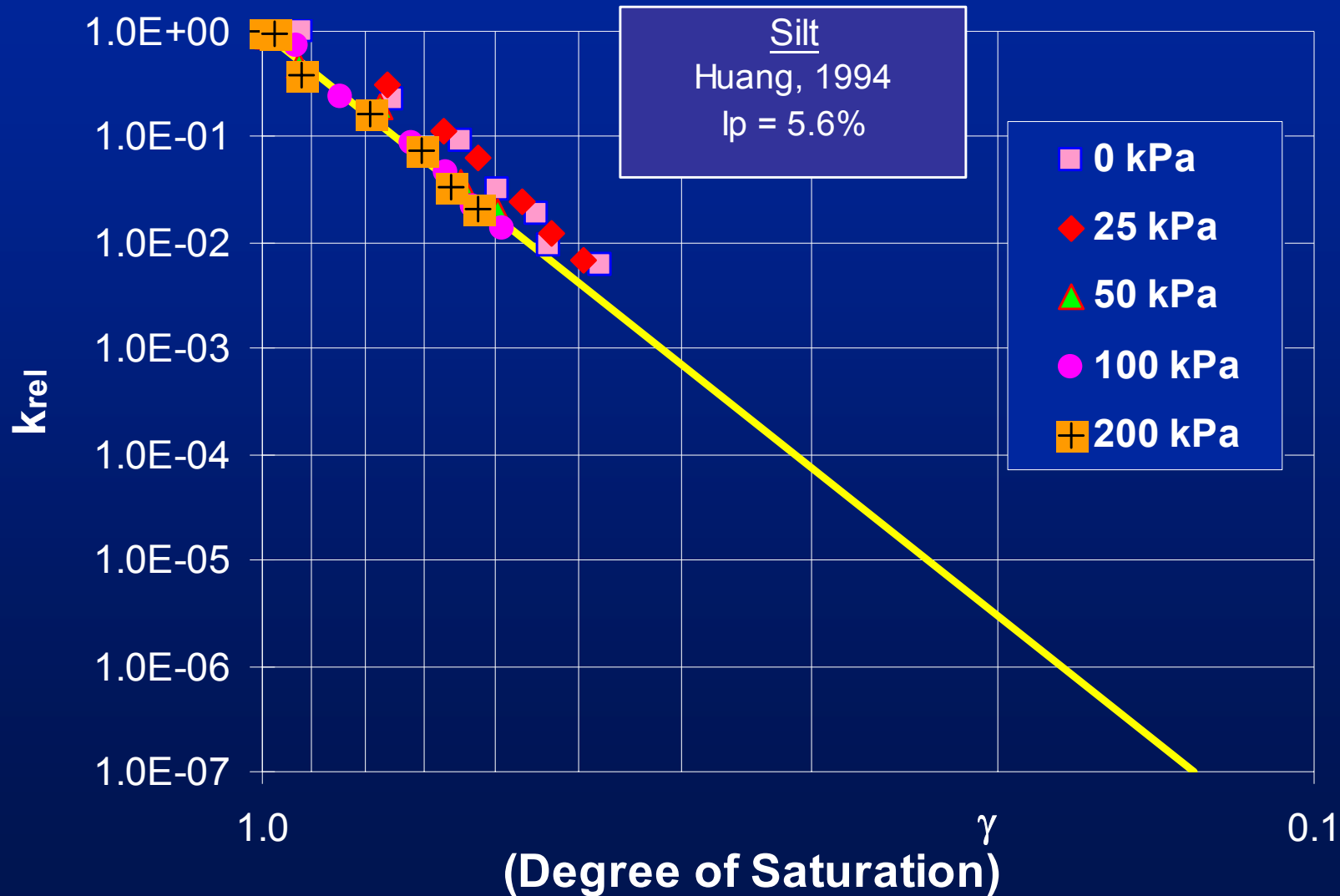


# $k_{rel}$ versus $S^\gamma$ for Yolo Light Clay

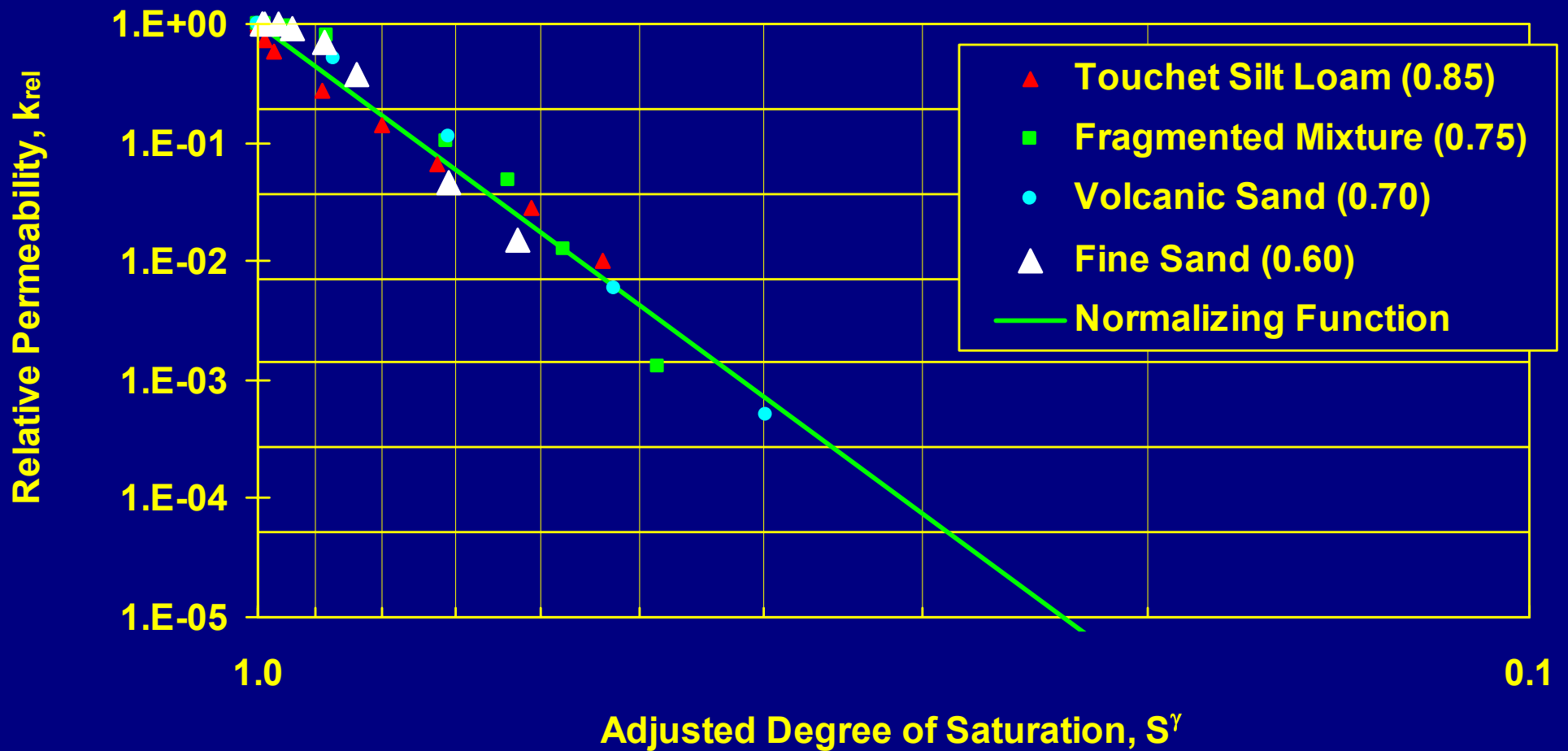




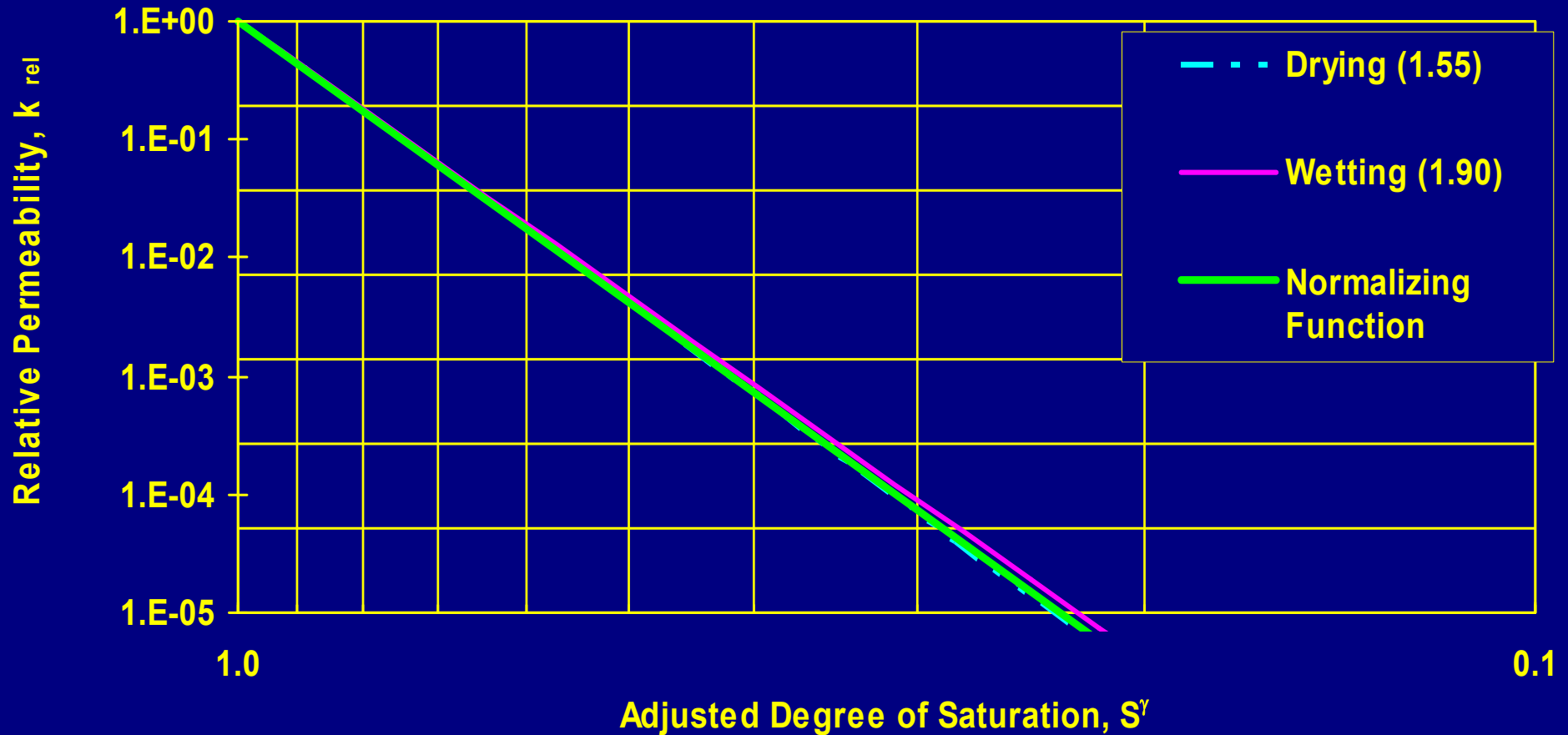
# *Influence of Stress State on the $k_{rel}$ versus $S^\gamma$ Relationship (Silt)*



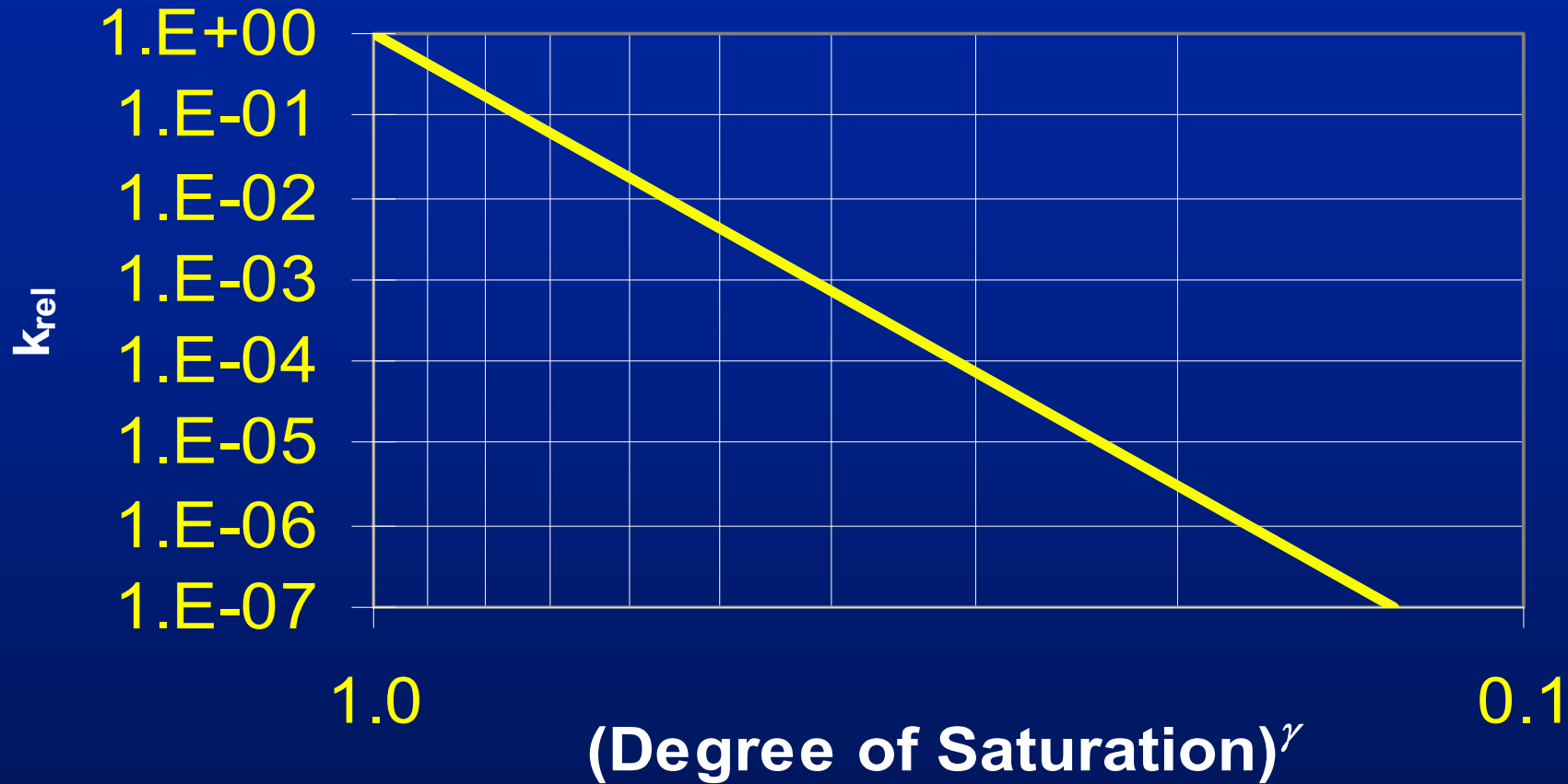
# $k_{rel}$ versus $S^{\gamma}$ for soils (Using Brooks & Corey 1964 Results)



# $k_{rel}$ versus $S^{\gamma}$ wetting & drying for London Clay (Croney & Coleman, 1954)



# The Relationship Between the $k_{rel}$ versus $S^\gamma$

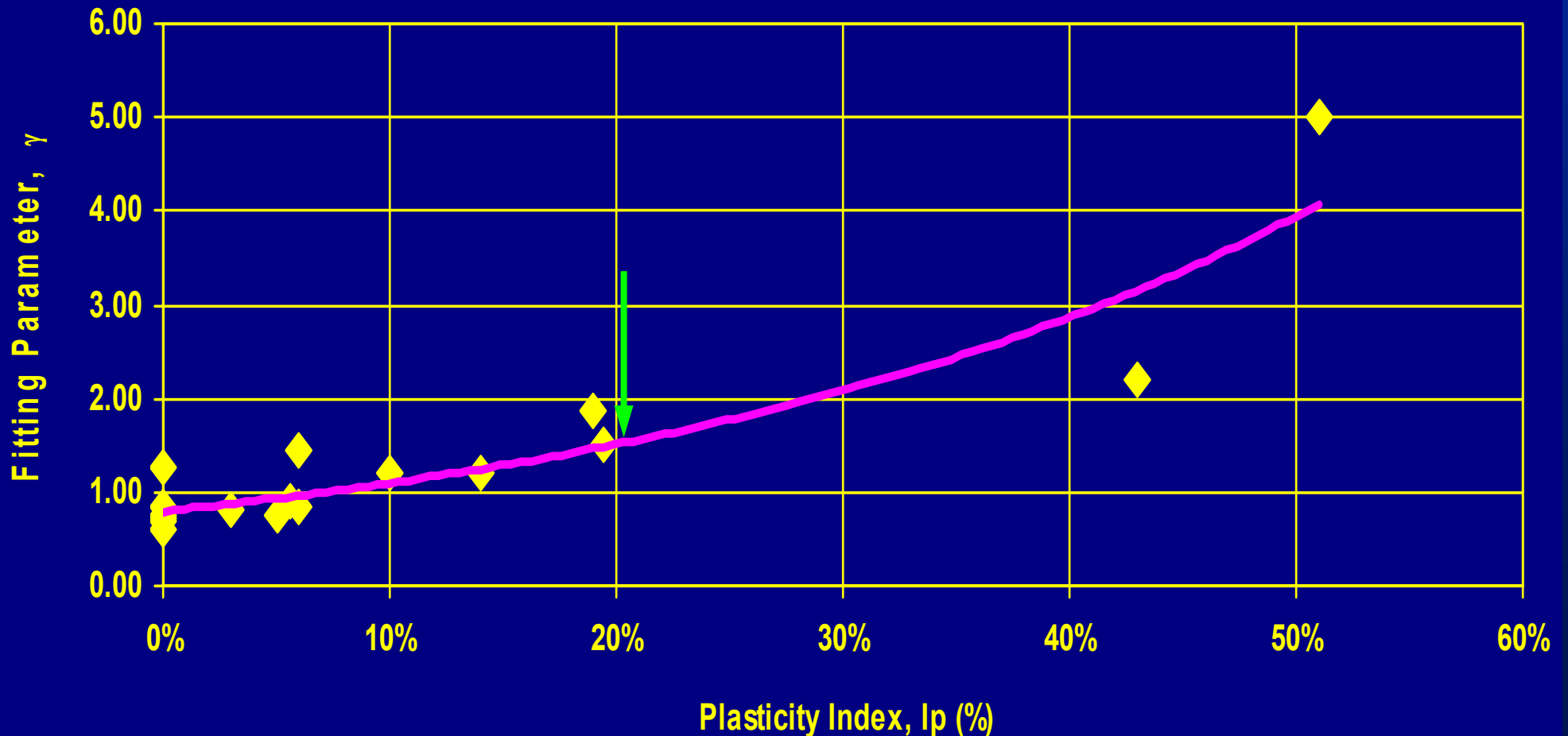


$$k_{rel} \approx S^{7.9\gamma}$$

where:

$$k_{rel} = k_{unsat}/k_{sat}$$

# *Relationship between Fitting Parameter $\gamma$ and Plasticity Index, $I_p$*



# ***Estimation of Unsaturated Coefficient of Permeability***

- The coefficient of permeability can be estimated using the simple function.

$$k_{rel} \approx S^{7.9\gamma}$$

- Required information: Saturated coefficient of permeability,  $k_{sat}$ , Water content,  $w$  or the degree of saturation,  $S$ , and the plasticity index,  $I_p$ .
- More studies are in progress to test the validity and the limitations of the proposed simple function.

# Summary

- SWCC can be used as a tool to propose simple estimation techniques for interpreting the engineering behavior of unsaturated soils.
- SWCC can be measured using centrifuge techniques reliably in a relatively shorter period of time compared to conventional procedures.
- The engineering properties of unsaturated soils can be estimated using simple techniques with the aid of conventional experimental results.
- These studies are useful to extend the principles of unsaturated soils into engineering practice such as the design of pavements

**Thank you,**



***Sai Vanapalli***  
***August 5, 2002***